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Introduction

The 2022 Oklahoma Academic Standards for Mathematics (OAS-M) are the result of the contributions of hundreds of mathematics educators and mathematicians from across the state of Oklahoma. This document reflects a balanced synthesis of the work of all members of the Oklahoma Academic Standards for Mathematics Writing Committee and feedback from educators, mathematicians, external reviews, and numerous education stakeholders.

The 2022 Oklahoma Academic Standards for Mathematics specify what students should know and be able to do as learners of mathematics at the end of each grade level or course. Students are held responsible for learning standards listed at earlier grade levels as well as at their current grade level. Throughout this document, the standards are written to allow time for study of additional material at every grade level. The order of the standards at any grade level is not meant to imply a sequence of topics and should be considered flexible for the organization of any course. The document provides standards for full-year PK-7, Pre-Algebra I, Geometry, Algebra II, Precalculus, and Statistics & Probability, with Algebra I as the prerequisite for both Geometry and Algebra II and Algebra II serving as the prerequisite for Precalculus and Statistics & Probability.

Development of the Oklahoma Academic Standards for Mathematics

The Oklahoma Academic Standards for Mathematics Review and Revision committees were informed by the 2016 Oklahoma Academic Standards for Mathematics, other states' standards documents and curriculum framework guides, and some of the latest research in mathematics education. The Oklahoma Academic Standards for Mathematics are neither curriculum nor instructional practices; standards serve as a foundation for curriculum.

- Standards: The concepts, content, and skills in which students should gain proficiency.
- **Curriculum:** The materials and resources used for teaching the standards.
- Instruction: The practices teachers use to deliver academic content to students. Teachers should utilize a variety of instructional techniques and strategies to ensure students master academic standards.

Oklahoma Math Curriculum Framework

Oklahoma educators have developed resources supporting a deeper understanding of the Oklahoma Academic Standards for Mathematics (OAS-M). Resources will be updated to reflect any revision to the OAS-M. To see resources and support for understanding and implementing the Oklahoma Academic Standards for Mathematics, explore the Oklahoma Math Curriculum Frameworks (bit.ly/OAS-M).

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Vision and Guiding Principles for the Understanding and Implementation of the OAS-M

The Oklahoma Academic Standards for Mathematics envision all students in Oklahoma will become mathematically proficient and literate through a strong mathematics program that emphasizes and engages them in problem solving, communicating, reasoning and proof, making connections, and using representations. Mathematically proficient and literate students can confidently and effectively use mathematics concepts, computation skills, and numbers to problem-solve, reason, and analyze information. Developing mathematical proficiency and literacy for Oklahoma students depends in large part on a clear, comprehensive, coherent, and developmentally appropriate set of standards to guide curricular decisions. The understanding and implementation of these standards throughout the PK-12 mathematics experience for students is based on the following guiding principles:

Guiding Principle 1: Excellence in mathematics education requires equity high expectations and strong support for all students.

All students must have opportunities to study–and support to learn – mathematics. Equity does not mean that every student should receive identical instruction; instead, it demands that reasonable and appropriate accommodations be made as needed to promote access and attainment for all students.

Guiding Principle 2: Mathematical ideas should be explored in ways that stimulate curiosity, create enjoyment of mathematics, and develop depth of understanding. Students need to understand mathematics deeply and use it effectively. To achieve mathematical understanding, students should be actively engaged in doing meaningful mathematics, discussing mathematical ideas, and applying mathematics in interesting, thought-provoking situations. Student understanding is further developed through ongoing reflection about cognitively demanding tasks relevant to their lives. Tasks should challenge and engage students in mathematics in multiple ways. Short- and long-term investigations that connect procedures and skills with conceptual understanding are integral components of an effective mathematics program. Activities should build upon curiosity and prior knowledge, and enable students to solve progressively deeper, broader, and more sophisticated problems. Tasks reflecting significant mathematics should generate active classroom talk, promote the development of conjectures and lead to an understanding of the necessity for mathematical reasoning.

Guiding Principle 3: An effective mathematics program focuses on problem solving. Mathematical problem solving is the hallmark of an effective mathematics program. Skill in mathematical problem solving requires practice with a variety of mathematical problems as well as a firm grasp of mathematical techniques and their underlying principles. Students who possess a deeper knowledge of mathematics can then use mathematics in a flexible way to tackle various problems and devise different ways of solving any problem. Mathematical problem solving calls for reflective thinking, persistence, and learning from the ideas of others. Success in solving mathematical problems helps to create an abiding interest in mathematics.

Guiding Principle 4: Technology is essential in teaching and learning

mathematics. Technology enhances the mathematics curriculum in many ways. Technology enables students to communicate ideas within the classroom or to search for needed information. It can be especially helpful in assisting students with special needs in regular and special education classrooms, at home, and in the community. Tools such as measuring instruments, manipulatives (e.g., base ten blocks and fraction pieces), online or hand-held scientific and graphing calculators, and computers with appropriate software, if properly used, contribute to a rich learning environment for developing and applying mathematical concepts. Appropriate use of calculators is essential; calculators should be used to enhance students' understanding and skills rather than replace them.



Reading the Oklahoma Academic Standards for Mathematics

Standards Overview

The Oklahoma Academic Standards for Mathematics are developed around four main content strands: Numbers and Operations, Algebraic Reasoning and Algebra, Geometry and Measurement, and Data and Probability. These four strands organize the content standards throughout PK-7 and Pre-Algebra. The standards for Algebra I, Algebra II, Geometry, Precalculus, and Statistics & Probability are also fundamentally organized around these strands. The Oklahoma Mathematical Actions and Processes (MAPs) are the skills and abilities students should develop and be engaged in throughout their PK-12 mathematics education. Among these are the ability to problem solve, communicate, and reason about mathematics, which will help students be ready for the mathematics expectations of college and the skills desired by many employers. While the MAPs and content standards work together to create clear, concise, and rigorous mathematics standards and expectations for Oklahoma students with the aim of helping them be college and career ready, it is not intended that each Mathematical Action and Process will be utilized or developed with each content standards that involve explaining a particular concept may be best accomplished by also engaging students in communicating mathematically, whereas standards that focus in the early grades on fluency with operations may align well with the Mathematical Action and Process focused on procedural fluency.

The Four Content Strands of the Oklahoma Academic Standards for Mathematics

Numbers and Operations Strand: A focus on numbers and operations is the cornerstone of a strong mathematics program. Developing students' fluency with numbers and operations throughout their PK-12 mathematics experience requires a balance and connection between conceptual understanding and computational proficiency and efficiency. This strand focuses on the importance of students' understanding of numbers, ways of representing numbers, relationships among numbers, relationships among number systems, and meanings of operations and how they relate to one another. An emphasis is placed on the development of estimation, so students can determine the reasonableness of solutions and answers. Further, it requires that students should be able to compute with proficiency and efficiency.



The Four Content Strands of the Oklahoma Academic Standards for Mathematics: continued

Algebraic Reasoning and Algebra Strand: All students should be able to reason algebraically and learn algebra. This strand provides focus for the PK-7 and Pre-Algebra standards around the notion that algebra is more than moving symbols around. It is about understanding patterns, relations, and functions, representing and analyzing mathematical situations and structures using algebraic symbols, using mathematical models to represent and understand quantitative relationships, and analyzing change in various contexts. These understandings are critical for success in college-level mathematics and fundamental for many real-world problems and situations students will face in their future careers. High school algebra, precalculus, and trigonometry standards use, apply, and extend these concepts.

Geometry and Measurement Strand: A focus on geometry should enable students to analyze characteristics of two- and threedimensional objects, develop arguments based on geometric relationships, describe spatial relationships using coordinate geometry and other representational systems, apply transformations and symmetry to analyze mathematical situations, and utilize visualization, spatial reasoning, and geometric modeling to solve problems. A focus on measurement should enable students to understand measurable attributes of objects and the units, systems, and processes of measurement, and apply appropriate techniques, tools, and formulas to determine measurements. This strand provides focus around the notion that geometry and measurement help students understand and represent ideas and solve problems they will encounter in their daily lives. The high school geometry standards use, apply, and extend these concepts.

Data and Probability Strand: An increased emphasis on understanding data should span all grade levels. Making sense of data and probability has become a part of our daily lives, supporting the importance of this strand throughout a student's PK-12 mathematics experience. A focus on data and probability should enable all students to formulate questions that can be addressed with data, and to collect, organize, and display relevant data to answer them. Students should select and use appropriate statistical methods to analyze data, develop and evaluate inferences and predictions that are based on data, and understand and apply basic concepts of probability. High school statistics and probability standards use, apply, and extend these concepts.

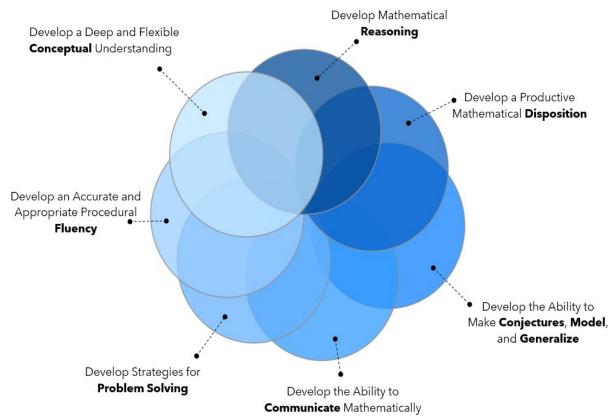


Standards vs. Objectives

The Oklahoma Academic Standards for Mathematics (OAS-M) consist of a set of standards and objectives (see page 9). The objectives serve as "stepping stones" for students to gain proficiency in the corresponding overarching standard. Each objective is the equivalent of at least one mathematical competency that students should know and be able to do if they can demonstrate proficiency in the standard. Objectives can and should be bundled to provide multiple opportunities and methods for students to learn and connect the standards and Mathematical Actions and Processes.

Mathematical Actions and Processes

The Mathematical Actions and Processes (MAPs) simultaneously reflect the holistic nature of mathematics as a discipline in which patterns and relationships among quantities, numbers, and space are studied and as a form of literacy such that all students are supported in accessing and understanding mathematics for life, for the workplace, for the scientific and technical community, and as a part of cultural heritage. The seven MAPS leverage both the NCTM Process Standards and the Five Mathematical Proficiencies to capture the mathematical experience of Oklahoma students as they pursue mathematical literacy. The gradient blocks at the top of each set of standards reminds educators to engage students in the Mathematical Actions and Processes together with content standards.





Mathematical Actions and Processes

Throughout their PK-12 education experience, mathematically literate students will:

Develop a Deep and Flexible Conceptual Understanding

Demonstrate a deep and flexible conceptual understanding of mathematical concepts, operations, and relations while making mathematical and real-world connections. Students will develop an understanding of how and when to apply and use the mathematics they know to solve problems.

Develop Accurate and Appropriate Procedural Fluency

Focus on the efficiency, flexibility, and accuracy in which students approach and solve problems. Students will learn and develop efficient procedures and algorithms for computations and repeated processes which includes developing fluency in operations with numbers and expressions. Students will have opportunities to justify both informal and commonly used strategies to support their choices of appropriate procedures. As they progress, students will strengthen their understanding and skill through application and practice.

Develop Strategies for Problem Solving

Analyze the parts of complex mathematical tasks and identify entry points to begin the search for a solution. Students will select from a variety of problem-solving strategies and use corresponding multiple representations (verbal, physical, symbolic, pictorial, graphical, tabular) when appropriate. They will pursue solutions to various tasks from realworld situations and applications that are often interdisciplinary in nature. They will find methods to verify their answers in context and will always question the reasonableness of solutions.

Develop Mathematical Reasoning

Explore and communicate a variety of reasoning strategies to think through problems. Students will apply their logic to critique the thinking and strategies of others to develop and evaluate mathematical arguments, including making arguments and counterarguments and making connections to other contexts.

Develop a Productive Mathematical Disposition

Hold the belief that mathematics is sensible, useful, and worthwhile. Students will develop the habit of looking for and making use of patterns and mathematical structures. They will persevere and become resilient, effective problem solvers.

Develop the Ability to Make Conjectures, Model, and Generalize

Make predictions and conjectures and draw conclusions throughout the problem-solving process based on patterns and the repeated structures in mathematics. Students will create, identify, and extend patterns as a strategy for solving and making sense of problems.

Develop the Ability to Communicate Mathematically

Students will discuss, write, read, interpret, and translate ideas and concepts mathematically. As they progress, students' ability to communicate mathematically will include their increased use of mathematical language and terms and analysis of mathematical definitions.



Reading the Oklahoma Academic Standards for Mathematics

			lahoma Acader	nic Standards fo	r Mathematic: 5 th C	GRADE OR C	OURSE		
MATH ACTIONS Develop a Deep and Flexible Conceptual Understanding	Develop Accur Appropria Procedural Fl	rate and D ate fo	Pevelop Strategies r Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability Communicate		
STANDARDS			Nu	mber & Operations	(N)				
5.N. 1 Read, write, represe compare fractions and dec			nt decimal fractions (e.g. relationship among fract	, 1/10, 1/100) usin ions, decimals and whole		prids, base-ten blocks, meter	stick) and showing the		
ecognize and write equiva ractions;convert between Ind decimals;use fractions lecimals in real-world and	fractions 5		ite, and represent decimers up to seven digits.	als using place value to d	escribe decimal numbers inclu	uding fractional numbers as s	mall as thousandths		
nathematical situations.	5	5. N.1.3 Compare	e and order fractions and	l decimals, including mixe	d numbers and fractions less t	han one, and locate on a nun	nber line.		
	5	5.N.1.4 Recogniz	ze and generate equival	ent decimals, fractions, mi	xed numbers, and fractions in	various mathematical model	s.		
. N.2 Divide multi-digit nu olve real-world and mathe roblems using arithmetic.	ematical 🔰 OI	BJECTIVE	nulti-digit numbers, by o	various mathematical mo ne- and two-digit divisors,	dels. based on knowledge of place	e value, including but not limi	ted to standard		
		.N.2.3 Recogniz	ze that remainders can b	e represented in a variety the context of the proble	of ways, including a whole nu m.	mber, fraction, or decimal. D	etermine the most		
	Va		s, including the inverse re	~	numbers problems requiring a rations, the use of technology,				
5.N.3 Add and subtract fractions with like and unlike denominators, mixed numbers and decimals to solve real- world and mathematical problems.		5.N.3.1 Estimate sums and differences of fractions with like and unlike denominators, mixed numbers, and decimals to assess the reasonableness of the results.							
		5.N.3.2 Illustrate addition and subtraction of fractions with like and unlike denominators, mixed numbers, and decimals using a variety of mathematical models (e.g., fraction strips, area models, number lines, fraction rods).							
	5	5.N.3.3 Add and subtract fractions with like and unlike denominators, mixed numbers, and decimals, involving money, measurement, geometry, and dat using various mathematical models including but not limited to standard algorithms.							
	5.	 Using various mathematical models including but not limited to standard algorithms. 5.N.3.4 Applying mental math and knowledge of place value (no computations), find 0.1 more than a number and 0.1 less than a number; find 0.01 more than a number and 0.01 less than a number. 							



Develop a Deep and Flexible Conceptual Understanding	ptual Appropriate Procedural		Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate		
			N	lumbers & Operations	(N)				
PK.N.1 Know number nar	mes and	PK.N.1.1 C	ount aloud forward in seque	ence by 1s to 20.					
count in sequence.		PK.N.1.2 Re	ecognize and name written r	numerals 0-10.					
		PK.N.1.3 Re	ecognize that 0 (zero) repres	sents the count of no objects.					
PK.N.2 Count to tell the n	number of			s, up to 10, in a row or colum					
objects.			•	nce in counting objects and r					
		PK.N.2.3 U	nderstand the last numeral s	spoken when counting aloud	tells how many total objects	are in a set up to 10.			
		PK.N.2.4 C	PK.N.2.4 Count up to 5 items in a scattered configuration, not in a row or column.						
PK.N.3 Compare sets usir	ng numbers.	PK.N.3.1 C	ompare two sets of 0-5 obje	ects using comparative langua	age such as "same," "more," c	or "fewer."			
			Algeb	oraic Reasoning & Alge	bra (A)				
PK.A.1 Recognize, duplic extend patterns.	ate, and		ort and group up to 5 objectommon.	ts into a set based upon cha	acteristics such as color, size	, and shape. Explain verbally	v what the objects have in		
		PK.A.1.2 Recognize, duplicate, and extend repeating patterns involving manipulatives, sound, movement, and other contexts.							
			Geon	netry & Measurement (GM)				
PK.GM.1 Identify commo	n shapes.	PK.GM.1.1	Identify circles, squares, rec	ctangles, and triangles by poi	nting to the shape when give	n the name.			
PK.GM.2 Describe and co	ompare	PK.GM.2.1 Identify measurable attributes of objects. Describe them using age-appropriate vocabulary (i.e., little, big, long, short, tall, heavy, light).							
measurable attributes.		PK.GM.2.2 Directly compare two objects with a common measurable attribute using age-appropriate vocabulary (e.g., longer/shorter, heavier/lighter, taller/shorter).							
	PK.GM.2.3 Sort objects into sets by one or more attributes.								
				Data & Probability (D)					
PK.D.1 Collect and organ	ize	PK.D.1.1 C	ollect and organize informat	tion about objects and events	in the environment.				
categorical data.		PK.D.1.2 U	se categorical data to create	e real-object graphs, with gui	dance and support.				



Develop a Deep and Flexible Conceptual Understanding	Develop Ac Appropriate Flue	Procedural	Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate				
	Numbers & Operations (N)										
K.N.1 Understand the related between quantities and whether the second	•		unt aloud forward in sequen	ce to 100 by 1s and 10s. e used to represent how man	v objects are in a set up to 10						
			-	ent the position of an object ir	· · ·						
		K.N.1.4 Red	cognize without counting (su	ubitize) the quantity of a small	group of objects in organized	and random arrangements	up to 10.				
		K.N.1.5 Co	unt forward, with and withou	ıt objects, from any given nun	nber up to 20.						
			ad, write, discuss, and repres tographs, spoken words, an	sent whole numbers from 0 to d manipulatives.	o at least 20. Representations	s may include numerals, pictu	ıres, real-object and				
		K.N.1.7 Fin	d a number that is 1 more or	r 1 less than a given number u	ip to 10.						
		K.N.1.8 Co	mpare and order whole num	nbers from 0 to 10 with and w	ithout objects, using the voca	bulary "more than," "less that	n," or "equal to."				
K.N.2 Develop conceptua understanding with additio subtraction (up to 10) usin and pictures.	ion and										
K.N.3 Understand the related between whole numbers at fractions through fair shared	and	K.N.3.1 Distribute a set of objects into at least two smaller equal sets.									
K.N.4 Identify coins by nar	me.	K.N.4.1 Ide	K.N.4.1 Identify pennies, nickels, dimes, and quarters by name.								
	Algebraic Reasoning & Algebra (A)										
K.A.1 Duplicate patterns i of contexts.	n a variety		t and group up to 10 objects nmon.	s into a set based upon charad	cteristics such as color, size, a	nd shape. Explain verbally wh	nat the objects have in				
			cognize, duplicate, complete lects, sounds, movement).	e, and extend repeating, incre	easing, and decreasing patte	rns in a variety of contexts (i.e	e., shape, color, size,				



	Geometry & Measurement (GM)					
K.GM.1 Recognize and sort basic	K.GM.1.1 Recognize squares, circles, triangles, and rectangles.					
two-dimensional shapes; use two- dimensional and three-dimensional	K.GM.1.2 Sort two-dimensional objects using characteristics such as shape and size.					
shapes to represent real-world objects.	K.GM.1.3 Identify attributes of two-dimensional shapes using informal and formal geometric language interchangeably, such as the number of corners/vertices and the number of sides/edges.					
	K.GM.1.4 Use smaller two-dimensional shapes to fill in the outline of a larger two-dimensional shape.					
	K.GM.1.5 Compose larger, undefined shapes and structures using three-dimensional objects.					
	K.GM.1.6 Use basic shapes and spatial reasoning to represent objects in the real world.					
K.GM.2 Compare and order objects	K.GM.2.1 Use words to compare objects according to length, size, weight, position, and location.					
according to location and measurable attributes.	K.GM.2.2 Order up to 6 objects using measurable attributes, such as length and weight.					
	K.GM.2.3 Identify more than one shared attribute between objects, and sort objects into sets.					
	K.GM.2.4 Compare the number of objects needed to fill two different containers.					
K.GM.3 Tell time as it relates to daily life.	K.GM.3.1 Develop an awareness of simple time concepts within daily life, using age-appropriate vocabulary (e.g., yesterday, today, tomorrow, morning, afternoon, night).					
	Data & Probability (D)					
K.D.1 Collect, organize, and	K.D.1.1 Collect and organize information about objects and events in the environment.					
interpret categorical data.	K.D.1.2 Use categorical data to create real-object graphs and pictographs.					
	K.D.1.3 Draw conclusions from real-object graphs and pictographs.					



Develop a Deep and Flexible Conceptual Understanding	Develop Ac Appropriate Flue	Procedural	Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate			
	Numbers & Operations (N)									
1.N.1 Count, compare, an represent whole numbers with an emphasis on group terms of tens and ones.	up to 100,	1.N.1.2 Use and	e concrete representations to d 100 is equivalent to 10 tens		tween 10 and 100 in terms o	f tens and ones. Know that 10	·			
		 1.N.1.3 Read, write, discuss, and represent whole numbers up to 100. Representations may include numerals, words, addition and subtraction, pictures, tally marks, number lines, and manipulatives. 1.N.1.4 Count forward, with objects, from any given number up to 100 by 1s, 2s, 5s and 10s. 1.N.1.5 Count forward, without objects, by multiples of 1s, 2s, 5s, and 10s, up to 100. 1.N.1.6 Find a number that is 10 more or 10 less than a given number up to 100. 								
		1.N.1.8 Use	 .N.1.7 Compare and order whole numbers from 0 to 100. .N.1.8 Use knowledge of number relationships to locate the position of a given whole number, up to 20, on an open number line. .N.1.9 Use words such as "more than," "less than," and "equal to" to describe the relative value of numbers. 							
and minuends of up to 10	ubtraction problems with sums and minuends of up to 10 in sal-world and mathematical									
1.N.3 Develop foundational ideas for fractions. 1.N.3.1 Partition a regular polygon using physical models and recognize when those parts are equal. 1.N.3.2 Partition (fair share) sets of objects into two and three equal groups.										
1.N.4 Identify coins and their values. 1.N.4.1 Identify pennies, nickels, dimes, and quarters by name and value. 1.N.4.2 Write a number with the cent symbol to describe the value of a coin. 1.N.4.3 Determine the value of a collection of pennies, nickels, or dimes up to one dollar, counting by 1s, 5s, and 10s.										



	Algebraic Reasoning & Algebra (A)					
1.A.1 Identify patterns found in real-world and mathematical problems.	1.A.1.1 Identify, create, complete, and extend repeating, increasing, and decreasing patterns in a variety of contexts (e.g., quantity, numbers, or shapes).					
	Geometry & Measurement (GM)					
1.GM.1 Recognize and compose two- and three-dimensional	1.GM.1.1 Identify regular and irregular trapezoids and hexagons by pointing to the shape when given the name.					
shapes.	1.GM.1.2 Compose larger, defined shapes using smaller two-dimensional shapes.					
	1.GM.1.3 Compose structures with three-dimensional shapes.					
	1.GM.1.4 Recognize three-dimensional shapes such as cubes, cones, cylinders, pyramids, and spheres.					
1.GM.2 Select and use nonstandard and standard units to describe length	1.GM.2.1 Use nonstandard and standard measuring tools to measure the length of objects.					
and volume/capacity.	1.GM.2.2 Illustrate that the length of an object is the number of same-size units of length that, when laid end-to-end with no gaps or overlaps, reach from one end of the object to the other.					
	1.GM.2.3 Measure the same object/distance with units of two different lengths, and describe how and why the measurements differ.					
	1.GM.2.4 Describe a length to the nearest whole unit using a number with standard and nonstandard units.					
	1.GM.2.5 Use standard and nonstandard tools to identify volume/capacity. Compare and sort containers that hold more, less, or the same amount.					
1.GM.3 Describe and measure concepts of time.	1.GM.3.1 Tell time to the hour and half-hour (analog and digital).					
or time.	1.GM.3.2 Describe and measure calendar time by days, weeks, months, and years.					
	Data & Probability (D)					
1.D.1 Collect, organize, and interpret categorical and numerical	1.D.1.1 Collect, sort, and organize data in up to three categories using representations (e.g., tally marks, tables, Venn diagrams).					
data.	1.D.1.2 Use data to create pictographs and bar graphs that demonstrate one-to-one correspondence.					
	1.D.1.3 Draw conclusions from pictographs and bar graphs.					



Develop a Deep and Flexible Conceptual Understanding Fluency		Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate				
	Numbers & Operations (N)									
2.N.1 Compare and represent numbers up to 1,000 with a	an emphasis		ad, write, discuss, and repres y marks, number lines, and r	sent whole numbers up to 1,0 manipulatives.	00. Representations should ir	nclude, but are not limited to,	numerals, words, pictures,			
on place value and equality	/.	2.N.1.2 Use	e knowledge of number relat	tionships to locate the positio	n of a given whole number, u	p to 100, on an open numbe	r line.			
				ole numbers between 10 and is equivalent to 10 ones and		tens, and ones, including writ	ten, standard, and			
		2.N.1.4 Fin	d 10 more or 10 less than a g	given three-digit number. Find	d 100 more or 100 less than a	given three-digit number.				
		2.N.1.5 Use	e objects to determine wheth	her a number is even or odd.						
			e place value understanding ations.	to round numbers to the near	est ten and nearest hundred	(up to 1,000). Recognize whe	n to round in real-world			
				d order whole numbers up to er page 350, 753 is between 7		iguage, numbers, and symbo	bls (e.g., 425 > 276,			
2.N.2 Add and subtract on		2.N.2.1 Use	e the relationship between a	ddition and subtraction to ger	nerate basic facts with sums a	nd minuends of up to 20.				
digit numbers in real-world mathematical problems.	land	2.N.2.2 Demonstrate fluency with basic facts of addition and subtraction with sums and minuends of up to 20.								
		2.N.2.3 Estimate sums and differences up to 100.								
		2.N.2.4 Use strategies and algorithms based on knowledge of place value and equality to add and subtract two-digit numbers.								
		2.N.2.5 Sol	ve addition and subtraction	problems involving whole nu	mbers up to two digits.					
		2.N.2.6 Use concrete models and structured arrangements, such as repeated addition, arrays, and ten frames to develop an understanding of multiplication.								
2.N.3 Explore the foundati	onal ideas of	2.N.3.1 Ide	entify the parts of a set and ar	ea that represent fractions for	halves, thirds, and fourths.					
fractions.		2.N.3.2 Construct equal-sized portions through fair sharing (length, set, and area models for halves, thirds, and fourths).								
2.N.4 Determine the value	of a set of	2.N.4.1 De	termine the value of a collect	tion of coins up to one dollar	using the cent symbol.					
coins.		2.N.4.2 Use	e a combination of coins to re	epresent a given amount of m	oney up to one dollar.					



	Algebraic Reasoning & Algebra (A)					
2.A.1 Describe the relationship found in	2.A.1.1 Represent, create, describe, complete, and extend increasing and decreasing patterns with quantity and numbers in a variety of contexts.					
patterns to solve real-world and mathematical problems.	2.A.1.2 Represent and describe repeating patterns involving shapes in a variety of contexts.					
2.A.2 Use number sentences involving	2.A.2.1 Use objects and number lines to represent number sentences.					
unknowns to represent and solve real- world and mathematical problems.	2.A.2.2 Generate models and situations to represent number sentences and vice versa.					
	2.A.2.3 Apply the commutative property, identity property, and number sense to find values for unknowns that make addition and subtraction number sentences true or false.					
	Geometry & Measurement (GM)					
2.GM.1 Analyze attributes of two- and	2.GM.1.1 Recognize regular and irregular trapezoids and hexagons.					
three-dimensional figures and develop generalizations about their	2.GM.1.2 Describe, compare, and classify two-dimensional figures according to their geometric attributes.					
properties.	2.GM.1.3 Compose and decompose two-dimensional shapes using triangles, squares, hexagons, trapezoids, and rhombi.					
	2.GM.1.4 Sort three-dimensional shapes based on attributes such as number of faces, vertices, and edges.					
	2.GM.1.5 Recognize right angles and classify angles as smaller or larger than a right angle.					
2.GM.2 Understand length as a	2.GM.2.1 Explain the relationship between the size of the unit of measurement and the number of units needed to measure the length of an object.					
measurable attribute and explore	2.GM.2.2 Explain the relationship between length and the numbers on a ruler by using a ruler to measure lengths to the nearest whole unit.					
capacity.	2.GM.2.3 Explore how varying shapes and styles of containers can have the same capacity.					
2.GM.3 Tell time to the quarter hour.	2.GM.3.1 Distinguish between a.m. and p.m.					
	2.GM.3.2 Read and write time to the quarter hour on an analog and digital clock.					
	Data & Probability (D)					
2.D.1 Collect, organize, and interpret data.	2.D.1.1 Explain that the length of a bar in a bar graph and the number of objects in a pictograph represents the number of data points for a given category.					
	2.D.1.2 Organize a collection of data with up to four categories using pictographs and bar graphs in intervals of 1s, 2s, 5s or 10s.					
	2.D.1.3 Write and solve one-step word problems involving addition or subtraction using data represented within pictographs and bar graphs with intervals of one.					
	2.D.1.4 Draw conclusions and make predictions from information in a pictograph and bar graph.					
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Develop a Deep and Flexible Conceptual Understanding	Develop Ac Appropriate Flue	Procedural	Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate		
Numbers & Operations (N)									
3.N.1 Compare and represent numbers up to 100,000 with the second seco	th an emphasis			ent whole numbers up to 100 ipulatives (e.g., 350 = 3 hund			o numerals, words,		
on place value and equality	у.		e place value to describe wh iding written, standard, and	ole numbers between 1,000 expanded forms.	and 100,000 in terms of ten t	housands, thousands, hundr	eds, tens and ones,		
				alues, use mental strategies (number, and 10,000 more or					
		3.N.1.4 Use	e place value to compare and	d order whole numbers, up to	100,000, using comparative	language, numbers, and sym	bols.		
		3.N.1.5 Use	e place value understanding	to round numbers to the near	rest thousand, ten-thousand a	and hundred thousand.			
3.N.2 Solve real-world and problems using addition, s	subtraction,	3.N.2.1 Represent multiplication facts by modeling a variety of approaches (e.g., manipulatives, repeated addition, equal-sized groups, arrays, area models, equal jumps on a number line, skip counting).							
multiplication, and division	1.	3.N.2.2 Demonstrate fluency with multiplication facts using factors up to 10.							
		3.N.2.3 Use strategies and algorithms based on knowledge of place value and equality to fluently add and subtract up to five-digit numbers (answer not to exceed 100,000).							
		3.N.2.4 Recognize when to round numbers and apply understanding to estimate sums and differences to the nearest ten thousand, thousand, hundred, and ten.							
		3.N.2.5 Use addition and subtraction to solve problems involving whole numbers. Use various strategies, including the relationship between addition and subtraction and the context of the problem to assess the reasonableness of results.							
		3.N.2.6 Represent division facts and divisibility by modeling a variety of approaches (e.g., repeated subtraction, equal sharing, forming equal groups) to show the relationship between multiplication and division.							
		3.N.2.7 Apply the relationship between multiplication and division to represent and solve problems.							
		3.N.2.8 Use various strategies (e.g., base ten blocks, area models, arrays, repeated addition, algorithms) based on knowledge of place value, equality, and properties of addition and multiplication to multiply a two-digit factor by a one-digit factor.							



3.N.3 Use and justify fractional	3.N.3.1 Read and write fractions with words and symbols using appropriate terminology (i.e., numerator and denominator).				
representations in real-world and mathematical problems.	3.N.3.2 Model fractions using length, set, and area for halves, thirds, fourths, sixths, and eighths.				
	3.N.3.3 Apply understanding of unit fractions and use this understanding to compose and decompose fractions related to the same whole.				
	3.N.3.4 Use models and number lines to order and compare fractions that are related to the same whole.				
3.N.4 Determine the value of a set of	3.N.4.1 Use addition and subtraction to determine the value of a collection of coins up to one dollar using the cent symbol and in monetary transactions.				
coins and determine the value of a set of bills in monetary transactions.	3.N.4.2 Add and subtract a collection of bills up to twenty dollars using whole dollars in monetary transactions.				
	Algebraic Reasoning & Algebra (A)				
3.A.1 Describe and create	3.A.1.1 Create, describe, and extend patterns involving addition, subtraction, or multiplication to solve problems in a variety of contexts.				
representations of numerical and geometric patterns.	3.A.1.2 Describe the rule (limited to a single operation) for a pattern from an input/output table or function machine involving addition, subtraction, or multiplication.				
	3.A.1.3 Explore and develop visual representations of increasing and decreasing geometric patterns and construct the next steps.				
3.A.2 Use number sentences involving multiplication and unknowns to	3.A.2.1 Use number sense with the properties of addition, subtraction, and multiplication, to find unknowns (represented by symbols) in one-step equations. Generate real-world situations to represent number sentences.				
represent and solve real-world and mathematical problems.	3.A.2.2 Identify, represent, and apply the number properties (commutative, identity, and associative properties of addition and multiplication) using models and manipulatives to solve problems.				
	Geometry & Measurement (GM)				
3.GM.1 Analyze and use geometric attributes to describe and create	3.GM 1.1 Sort three-dimensional shapes based on attributes.				
polygons and three-dimensional figures in various contexts.	3.GM.1.2 Build a three-dimensional figure using unit cubes when shown a picture of a three-dimensional shape.				
in various contexts.	3.GM.1.3 Classify angles within a polygon as acute, right, obtuse, and straight.				
3.GM.2 Understand measurable attributes of real-world and mathematical	3.GM.2.1 Find the perimeter of a polygon, given whole number lengths of the sides, using a variety of models.				
objects using various tools.	3.GM.2.2 Analyze why length and width are multiplied to find the area of a rectangle by decomposing the rectangle into one unit by one unit squares and viewing these as rows and columns to determine the area.				
	3.GM.2.3 Count cubes systematically to identify the number of cubes needed to pack the whole or half of a three-dimensional structure.				
	3.GM.2.4 Find the area of two-dimensional figures by counting the total number of same-size unit squares that fill the shape without gaps or overlaps.				



3.GM.2 continued Understand measurable attributes of real-world and	3.GM.2.5 Choose an appropriate measurement instrument and measure the length of objects to the nearest whole centimeter or whole meter.			
mathematical objects using various tools.	3.GM.2.6 Choose an appropriate measurement instrument and measure the length of objects to the nearest whole yard, whole foot, or half inch.			
	3.GM.2.7 Use an analog thermometer to determine temperature to the nearest degree in Fahrenheit and Celsius.			
3.GM.3 Solve problems by telling time to the nearest five-minute interval.	3.GM.3.1 Read and write time to the nearest five-minute interval (analog and digital).			
	3.GM.3.2 Determine the solutions to problems involving addition and subtraction of time in intervals of five minutes, up to one hour, using pictorial models, number line diagrams, or other tools.			
	Data & Probability (D)			
3.D.1 Collect, organize, and analyze	3.D.1.1 Collect and organize a data set with multiple categories using a frequency table, line plot, pictograph, or bar graph with scaled intervals.			
data.	3.D.1.2 Solve one- and two-step problems using categorical data represented with a frequency table, pictograph, or bar graph with scaled intervals.			



Develop a Deep and Flexible Conceptual Understanding	Develop Accurate and Appropriate Procedural Fluency		Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate	
	Numbers & Operations (N)							
4.N.1 Compare and represent numbers up to 1,000,000 w	with an	4.N.1.1 Read, write, discuss, and represent whole numbers up to 1,000,000. Representations may include numerals, words, pictures, number lines, and manipulatives.						
emphasis on place value ar	nd equality.		•	ole numbers between 1,000 written, standard, and expand		lions, hundred thousands, te	en thousands, thousands,	
		4.N.1.3 Ap	plying knowledge of place v	alue, use mental strategies (n	o written computations) to m	ultiply or divide a number by	y 10, 100 and 1,000.	
		4.N.1.4 Use	e place value to compare and	order whole numbers up to	1,000,000, using comparative	language, numbers, and syr	nbols.	
4.N.2 Solve real-world and	1	4.N.2.1 Der	monstrate fluency with multip	olication and division facts wit	h factors up to 12.			
mathematical problems us multiplication and division.	•	4.N.2.2 Multiply 3-digit by 1-digit and 2-digit by 2-digit whole numbers, using various strategies, including but not limited to standard algorithms.						
		4.N.2.3 Estimate products of 3-digit by 1-digit and 2-digit by 2-digit whole number factors using a variety of strategies (e.g., rounding, front end estimation, adjusting, compatible numbers) to assess the reasonableness of results. Explore larger numbers using technology to investigate patterns.						
		4.N.2.4 Apply and analyze models to solve multi-step problems requiring the use of addition, subtraction, and multiplication of multi- digit whole numbers. Use various strategies, including the relationship between operations, the use of appropriate technology, and the context of the problem to assess the reasonableness of results.						
4.N.2.5 Use strategies and algorithms (e.g., mental strategies, standard algorithms, partial quotients, repeated subtraction, the commutative, associative, and distributive properties) based on knowledge of place value, equality, and properties of operations to divide a 3-digit dividend by a 1-digit whole number divisor, with and without remainders.								
4.N.3 Represent and com		4.N.3.1 Represent and rename equivalent fractions using fraction models (e.g., parts of a set, area models, fraction strips, number lines).						
and decimals in real-world and mathematical situations; use place	se place	4.N.3.2 Use benchmark fractions $(0, \frac{1}{4}, \frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \frac{3}{4}, 1)$ to locate additional fractions with denominators up to twelfths on a number line.						
value to understand decimal quantities.		4.N.3.3 Use models to order and compare whole numbers and fractions less than and greater than one, using comparative language and symbols.						
				m of fractions with the same c ical representations (e.g., $\frac{3}{4}$ =		e way, using concrete and pi	ctorial models	



4.N.3 <i>continued</i> Represent and compare fractions and decimals in real-world and mathematical situations; use place value to understand decimal	4.N.3.5 Use models to add and subtract fractions with like denominators.				
	4.N.3.6 Represent tenths and hundredths with concrete and pictorial models, making connections between fractions and decimals.				
quantities.	4.N.3.7 Read and write decimals in standard, word, and expanded form up to at least the hundredths place in a variety of contexts, including money.				
	4.N.3.8 Compare and order decimals and whole numbers using place value and various models including but not limited to grids, number lines, and base 10 blocks.				
	4.N.3.9 Compare and order benchmark fractions $(0, \frac{1}{4}, \frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \frac{3}{4}, 1)$ and decimals $(0, 0.25, 0.50, 0.75, 1.00)$ in a variety of representations.				
4.N.4 Determine the value of bills and	4.N.4.1 Select the fewest number of coins for a given amount of money up to one dollar.				
coins in order to solve monetary transactions.	4.N.4.2 Given a total cost (dollars and coins up to twenty dollars) and amount paid (dollars and coins up to twenty dollars), find the change required in a variety of ways.				
	Algebraic Reasoning & Algebra (A)				
4.A.1 Describe, create, and analyze	4.A.1.1 Create an input/output chart or table to represent or extend a numerical pattern.				
multiple representations of patterns to solve real-world and mathematical	4.A.1.2 Describe the single operation rule for a pattern from an input/output table or function machine involving any operation of a whole number.				
problems.	4.A.1.3 Construct models to show growth patterns involving geometric shapes and define the single operation rule of the pattern.				
4.A.2 Use multiplication and division with variables to create number	4.A.2.1 Use the relationships between multiplication and division with the properties of multiplication to solve problems and find values for variables that make number sentences true.				
sentences representing a given mathematical situation.	4.A.2.2 Solve for a variable in an equation involving addition, subtraction, multiplication, or division with whole numbers. Analyze models to represent number sentences and vice versa.				
	4.A.2.3 Determine the unknown addend or factor in equivalent and non-equivalent expressions (e.g., $5 + 6 = 4 + \Box$, $3 \cdot 8 < 3 \cdot \Box$).				
	Geometry & Measurement (GM)				
4.GM.1 Name, describe, classify, and	4.GM.1.1 Identify points, lines, line segments, rays, angles, endpoints, and parallel and perpendicular lines in various models.				
construct polygons and three- dimensional figures based on their attributes; recognize polygons and three-dimensional figures in real-life and mathematical situations.	4.GM.1.2 Describe, classify, and construct quadrilaterals, including squares, rectangles, trapezoids, rhombuses, parallelograms, and kites. Recognize quadrilaterals in various models.				
	4.GM.1.3 Given two three-dimensional shapes, identify each shape. Compare and contrast their similarities and differences based on their attributes.				



4.GM.2 Recognize and measure attributes in real-world and	4.GM.2.1 Measure angles in geometric figures and real-world objects with a protractor or angle ruler.				
mathematical situations using various tools.	4.GM.2.2 Find the area of polygons by determining if they can be decomposed into rectangles.				
	4.GM.2.3 Develop the concept that the volume of rectangular prisms with whole-number edge lengths can be found by counting the total number of same-sized unit cubes that fill a shape without gaps or overlaps. Use a variety of tools and create models to determine the volume using appropriate measurements (e.g., cm ³).				
	4.GM.2.4 Choose an appropriate instrument to measure the length of an object to the nearest whole centimeter or quarter inch.				
	4.GM.2.5 Recognize and use the relationship between inches, feet, and yards to measure and compare objects.				
	4.GM.2.6 Recognize and use the relationship between millimeters, centimeters, and meters to measure and compare objects.				
	4.GM.2.7 Determine and justify the best use of customary and metric measurements in a variety of situations (liquid volumes, mass vs. weight, temperatures above 0 (zero) degrees, and length).				
4.GM.3 Determine elapsed time	4.GM.3.1 Determine elapsed time.				
andconvert between units of time.	4.GM.3.2 Convert one measure of time to another including seconds to minutes, minutes to hours, hours to days, and vice versa, using various models.				
	Data & Probability (D)				
4.D.1 Summarize, construct, and analyze data.	4.D.1.1 Create and organize data on a frequency table or line plot marked with whole numbers and fractions using appropriate titles, labels, and units.				
	4.D.1.2 Organize data sets to create tables, bar graphs, timelines, and Venn diagrams. The data may include benchmark fractions or decimals $(\frac{1}{4}, \frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \frac{3}{4}, 0.25, 0.50, 0.75)$.				
	4.D.1.3 Solve one- and two-step problems by analyzing data in whole number, decimal, or fraction form in a frequency table and line plot.				



Develop a Deep and Flexible Conceptual Understanding	Develop Acc Appropriate Fluer	Procedural	Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate
			٩	Numbers & Operations	(N)		
5.N.1 Read, write, represent compare fractions and dec recognize and write equivat fractions; convert between	imals; Ilent fractions	nur 5.N.1.2 Rea	mber relationships among fra	actions, decimals and whole mals using place value to des	els (e.g., 10 by 10 grids, base-t numbers. cribe decimal numbers incluc		
and decimals; use fractions decimals in real-world and mathematical situations.	and	5.N.1.3 Co	mpare and order decimals a	nd fractions, including mixed	numbers and fractions less th actions, mixed numbers, and f		ber line.
5.N.2 Divide multi-digit numbers and solve real-world and mathematical problems using arithmetic.		 5.N.2.1 Estimate solutions to division problems to assess the reasonableness of results. 5.N.2.2 Divide multi-digit numbers, by one- and two-digit divisors, based on knowledge of place value, including but not limited to standard algorithms. 					
		5.N.2.3 Recognize that remainders can be represented in a variety of ways, including a whole number, fraction, or decimal. Determine the most meaningful form of a remainder based on the context of the problem.					
		5.N.2.4 Construct models to solve multi-digit whole number problems requiring addition, subtraction, multiplication, and division using various representations, including the inverse relationships between operations, the use of technology, and the context of the problem to assess the reasonableness of results.					
5.N.3 Add and subtract fractions with like and unlike denominators, mixed numbers, and decimals to solve real-world and mathematical problems.		5.N.3.1 Estimate sums and differences of fractions with like and unlike denominators, mixed numbers, and decimals to assess the reasonableness of the results.					the reasonableness of the
		5.N.3.2 Illustrate addition and subtraction of fractions with like and unlike denominators, mixed numbers, and decimals using a variety of mathematical models (e.g., fraction strips, area models, number lines, fraction rods).					
		5.N.3.3 Add and subtract fractions with like and unlike denominators, mixed numbers, and decimals, involving money, measurement, geometry, and data. Use various models and efficient strategies, including but not limited to standard algorithms.					
5.N.3.4 Apply mental math and knowledge of place value (no written computations) to find 0.1 more or 0.1 less than a number, 0.01 more or 0.01 less than a number. a number, and 0.001 more or 0.001 less than a number.					0.01 more or 0.01 less than		



	Algebraic Reasoning & Algebra (A)
5.A.1 Describe and graph patterns of change created through numerical	5.A.1.1 Use tables and rules with up to two operations to describe patterns of change and make predictions and generalizations about various mathematical situations.
patterns.	5.A.1.2 Use a rule or table to represent ordered pairs of whole numbers and graph these ordered pairs on a coordinate plane, identifying the origin and axes in relation to the coordinates.
5.A.2 Understand and interpret expressions, equations, and inequalities	5.A.2.1 Generate equivalent numerical expressions and solve problems using number sense involving whole numbers by applying the commutative property, associative property, distributive property, and order of operations (excluding exponents).
involving variables and whole numbers, and use them to represent and evaluate	5.A.2.2 Determine whether an equation or inequality involving a variable is true or false for a given value of the variable.
real-world and mathematical problems.	5.A.2.3 Evaluate expressions involving variables when values for the variables are given.
	Geometry & Measurement (GM)
5.GM.1 Describe, identify, classify, and construct two- and three-	5.GM.1.1 Describe, identify, classify, and construct triangles (equilateral, right, scalene, isosceles) by their attributes using various mathematical models.
dimensional figures using their geometric attributes.	5.GM.1.2 Describe, identify, and classify three-dimensional figures (cubes, rectangular prisms, and pyramids) and their attributes (number of edges, faces, vertices, shapes of faces), given various mathematical models.
	5.GM.1.3 Recognize and draw a net for a three-dimensional figure (cube, rectangular prism, pyramid).
5.GM.2 Determine volume using the object's dimensions. Compare and	5.GM.2.1 Determine the volume of rectangular prisms by the number of unit cubes (<i>n</i>) used to construct the shape and by the product of the dimensions of the prism $a \cdot b \cdot c = n$. Understand rectangular prisms of different dimensions (<i>p</i> , <i>q</i> , and <i>r</i>) can have the same volume if $a \cdot b \cdot c = p \cdot q \cdot r = n$.
analyze rectangular prisms with equivalent volume to recognize their different dimensions.	5.GM.2.2 Estimate the perimeter of polygons and create arguments for reasonable perimeter values of shapes that may include curves.
5.GM.3 Understand angle, length,	5.GM.3.1 Measure and compare angles according to size using various tools.
weight, and capacity as measurable attributes of real-world and mathematical	5.GM.3.2 Measure the length of an object to the nearest whole centimeter or up to 1/16 inch using an appropriate instrument.
objects, using various tools to measure	5.GM.3.3 Apply the relationship between inches, feet, and yards to measure, convert, and compare objects to solve problems.
them. Solve real-world problems of length.	5.GM.3.4 Apply the relationship between millimeters, centimeters, and meters to measure, convert, and compare objects to solve problems.
lengen	5.GM.3.5 Estimate lengths and geometric measurements to the nearest whole unit, using benchmarks in customary and metric measurement systems.
	Data & Probability (D)
5.D.1 Create and analyze data to find the range and measures of central	5.D.1.1 Find the measures of central tendency (i.e., mean, median, mode) and range of a set of data. Understand that the mean is a "leveling out" or central balance point of the data.
tendency (mean, median, mode).	5.D.1.2 Create and analyze line and double-bar graphs with increments of whole numbers, fractions, and decimals.



Develop a Deep and Flexible Conceptual Understanding	Flexible Conceptual Appropriate Procedural		Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate	
			Π	Numbers & Operations	(N)			
6.N.1 Read, write, and repr numbers expressed as inte				(e.g., number lines) to deterr zero) in a variety of situations.	nine positive and negative nu	umbers and their contexts, id	entify opposites,	
fractions, decimals, percenture these representations i		6.N.1.2 Co	mpare and order positive rat	tional numbers, represented i	n various forms, or integers u	sing the symbols "<", ">", and	d "=".	
and mathematical situation	IS.		· · ·	ts parts "out of 100" and ratio				
				g fractions, mixed numbers, c				
6.N.2 Read, write, and mod number and integer operat				ddition and subtraction of pro		reasonableness of results.		
problems.			6.N.2.2 Illustrate addition and subtraction of integers using a variety of representations.6.N.2.3 Add and subtract integers in a variety of situations; use efficient and generalizable procedures including but not limited to standard algorithms.					
		6.N.2.4 Identify and represent patterns with whole-number exponents and perfect squares. Evaluate powers with whole-number bases and exponents.						
		6.N.2.5 Fac	ctor whole numbers and exp	ress prime and composite nu	mbers as a product of prime f	factors with exponents.		
				n factors and least common n ss the sum of two-digit numb		s and multiples to calculate w ng the distributive property.	ith fractions, find	
6.N.3 Explain and use the concept of ratio and its relationship to other		6.N.3.1 Identify and use ratios to compare and relate quantities in multiple ways. Recognize that multiplicative comparison and additive comparison are different.						
rational numbers and to the multiplication and division	e	6.N.3.2 Determine the unit rate for ratios.						
numbers. Use ratios to solve		6.N.3.3 Ap	ply the relationship between	ratios, equivalent fractions, u	nit rates, and percents to solv	e problems in various contex	ts.	
6.N.4 Multiply and divide of fractions, and mixed number of the second		6.N.4.1 Estimate solutions to problems with whole numbers, decimals, fractions, and mixed numbers, and use the estimates to assess the reasonableness of results in the context of the problem.						
world and mathematical problems with rational numbers.		6.N.4.2 Illustrate multiplication and division of fractions and decimals to show connections to fractions, whole number multiplication, and inverse relationships.						
		6.N.4.3 Multiply and divide fractions and decimals using efficient and generalizable procedures.						
 6.N.4.4 Use mathematical modeling to solve and interpret problems including money, measurement, geometry, and data requiring arithmetic with decimals, fractions and mixed numbers. 					iring arithmetic with			



	Algebraic Reasoning & Algebra (A)
6.A.1 Recognize and represent relationships between varying	6.A.1.1 Plot integer- and rational-valued (limited to halves and fourths) ordered-pairs as coordinates in all four quadrants and recognize the reflective relationships among coordinates that differ only by their signs.
quantities; translate from one representation to another; use patterns,	6.A.1.2 Represent relationships between two varying positive quantities involving no more than two operations with rules, graphs, and tables; translate between any two of these representations.
tables, graphs, and rules to model and solve mathematical problems.	6.A.1.3 Use and evaluate variables in expressions, equations, and inequalities that arise from various contexts, including determining when or if, for a given value of the variable, an equation or inequality involving a variable is true or false.
6.A.2 Use properties of arithmetic to generate equivalent numerical expressions and evaluate expressions involving positive rational numbers.	6.A.2.1 Generate equivalent expressions and evaluate expressions involving positive rational numbers by applying the commutative, associative, and distributive properties and order of operations to model and solve mathematical problems.
6.A.3 Use equations and inequalities to	6.A.3.1 Model mathematical situations using expressions, equations and inequalities involving variables and rational numbers.
model and solve mathematical problems and use the idea of maintaining equality to solve equations. Interpret solutions in the original context.	6.A.3.2 Use number sense and properties of operations and equality to model and solve mathematical problems involving equations in the form $x + p = q$ and $px = q$, where p and q are nonnegative rational numbers. Graph the solution on a number line, interpret the solution in the original context, and assess the reasonableness of the solution.
	Geometry & Measurement (GM)
6.GM.1 Use translations, reflections, and	6.GM.1.1 Predict, describe, and apply translations (slides), reflections (flips), and rotations (turns) to a two-dimensional figure.
rotations to establish congruence and understand symmetry (not on a	6.GM.1.2 Recognize that translations, reflections, and rotations preserve congruence and use them to show that two figures are congruent.
coordinate plane).	6.GM.1.3 Identify and describe the line(s) of symmetry in two-dimensional shapes.
6.GM.2 Use mathematical modeling to calculate the area of squares,	6.GM.2.1 Develop and use formulas for the area of squares and parallelograms using a variety of methods including but not limited to the standard algorithms and finding unknown measures.
parallelograms, and triangles to solve	6.GM.2.2 Develop and use formulas to determine the area of triangles and find unknown measures.
problems.	6.GM.2.3 Find the area of right triangles, other triangles, special quadrilaterals, and polygons that can be decomposed into triangles and other shapes.
6.GM.3 Understand and use	6.GM.3.1 Solve problems using the relationships between the angles (vertical, complementary, and supplementary) formed by intersecting lines.
relationships between angles in geometric figures.	6.GM.3.2 Develop and use the fact that the sum of the interior angles of a triangle is 180° to determine missing angle measures in a triangle.
6.GM.4 Choose appropriate units of	6.GM.4.1 Estimate weights and capacities using benchmarks in customary and metric measurement systems with appropriate units.
measurement and use ratios to convert within measurement systems to model and solve real-world and mathematical problems.	6.GM.4.2 Solve problems that require the conversion of lengths within the same measurement systems using appropriate units.



	Data & Probability (D)					
6.D.1 Interpret and analyze data.	bret and analyze data. 6.D.1.1 Interpret the mean, median, and mode for a set of data.					
	6.D.1.2 Explain and justify which measure of center (mean, median, or mode) would provide the most descriptive information for a given set of data.					
6.D.2 Use probability to model and	6.D.2.1 Represent possible outcomes using a probability continuum from impossible to certain.					
solve mathematical problems; represent probabilities using fractions and decimals.	6.D.2.2 Determine the sample space for a given experiment and determine which members of the sample space are related to certain events. Sample space may be determined by the use of tree diagrams, tables or pictorial representations.					
	6.D.2.3 Demonstrate simple experiments in which the probabilities are known and compare the resulting relative frequencies with the known probabilities, recognizing that there may be differences between the two results.					



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	Numbers & Operations (N)							
7.N.1 Read, write, represent,		7.N.1.1 Co	mpare and order rational nur	mbers expressed in various f	orms using the symbols "<", "	>", and "=".		
compare rational numbers, e integers, fractions, and decim	nals. Explain	7.N.1.2 Rec	cognize and generate equival	ent representations of ration	al numbers, including equival	ent fractions.		
and apply the concept of abso	olute value.				onal number and the distance alue to model and solve prob		a number line. Use the	
7.N.2 Calculate with rational		7.N.2.1 Esti	imate solutions to multiplicati	ion and division of integers i	n order to assess the reasonab	leness of results.		
with and without positive inte exponents, to model and solv		7.N.2.2 Illus	strate multiplication and divis	ion of integers using a variet	y of representations.			
mathematical problems.		7.N.2.3 Mu	7.N.2.3 Multiply and divide integers in a variety of situations; use efficient and generalizable procedures, including standard algorithms.					
		7.N.2.4 Raise rational numbers (integers, fractions, and decimals) to positive integer exponents.						
		7.N.2.5 Mo	del and solve problems using	g rational numbers involving	addition, subtraction, multip	lication, division, and positiv	e integer exponents.	
			Algeb	raic Reasoning & Alge	bra (A)			
7.A.1 Explain the concept of proportionality in mathematical models and situations and distinguish between proportional and non-proportional relationships.		7.A.1.1 Identify a relationship between two varying quantities, x and y, as proportional if it can be expressed in the form $\frac{y}{x} = k$ or $y = kx$; distinguish proportional relationships from non-proportional relationships.						
		7.A.1.2 Recognize that the graph of a proportional relationship is a line through the origin and the coordinate (1, <i>r</i>), where <i>r</i> is the slope and the unit rate (constant of proportionality, <i>k</i>).						
7.A.2 Identify and justify proportional relationships using mathematical models and situations; solve problems involving proportional relationships and interpret results in the original context.		7.A.2.1 Represent proportional relationships with tables, verbal descriptions, symbols, and graphs; translate from one representation to another. Determine and compare the unit rate (constant of proportionality, slope, or rate of change) given any of these representations.						
		7.A.2.2 Solve multi-step problems with proportional relationships (e.g., distance-time, percent increase or decrease, discounts, tips, unit pricing, mixtures and concentrations, similar figures, other mathematical situations).						
		7.A.2.3 Use proportional reasoning to solve problems involving ratios.						
7.A.2.4 Use proportional reasoning to assess the reasonableness of solutions.								



7.A.3 Represent mathematical situations using equations and inequalities involving	7.A.3.1 Write and solve problems leading to linear equations with one variable in the form $px + q = r$ and $p(x + q) = r$, where p , q , and r are rational numbers.
variables and rational numbers.	7.A.3.2 Represent, write, solve, and graph problems leading to linear inequalities with one variable in the form $x + p > q$ and $x + p < q$, where p , and q are nonnegative rational numbers.
7.A.4 Use order of operations and properties of operations to generate and	7.A.4.1 Use properties of operations (associative, commutative, and distributive) to generate equivalent numerical and algebraic expressions containing rational numbers, grouping symbols and whole number exponents.
evaluate equivalent numerical and algebraic expressions.	7.A.4.2 Evaluate numerical expressions using calculators and other technologies and justify solutions using order of operations and grouping symbols.
	Geometry & Measurement (GM)
7.GM.1 Develop and understand the	7.GM.1.1 Recognize that the surface area of a rectangular prism can be found by finding the area of each component of the net of that figure. Know that rectangular prisms of different dimensions can have the same surface area.
concept of surface area and volume of rectangular prisms with rational-valued	7.GM.1.2 Using a variety of tools and strategies, develop the concept that surface area of a rectangular prism can be found by wrapping the figure with same-sized square units without gaps or overlap. Use appropriate measurements (e.g., cm ²).
edge lengths.	7.GM.1.3 Using a variety of tools and strategies, develop the concept that the volume of rectangular prisms can be found by counting the total number of same-sized unit cubes that fill a shape without gaps or overlaps. Use appropriate measurements (e.g., cm ³).
7.GM.2 Use mathematical models and problems to calculate and justify	7.GM.2.1 Develop and use the formula to determine the area of a trapezoid.
the area of trapezoids and the area and perimeter of composite figures with rational measurements.	7.GM.2.2 Find the area and perimeter of composite figures.
7.GM.3 Use mathematical models and	7.GM.3.1 Solve problems that require the conversion of weights and capacities within the same measurement systems using appropriate units.
reasoning with proportions and ratios to determine measurements, justify formulas, and solve problems.	7.GM.3.2 Demonstrate an understanding of the proportional relationship between the diameter and circumference of a circle and that the unit rate (constant of proportionality) is pi (π) and can be approximated by rational numbers such as $\frac{22}{7}$ and 3.14.
	7.GM.3.3 Calculate the circumference and area of circles to solve problems in various contexts, in terms of pi (π) and using approximations for pi (π).
7.GM.4 Analyze the effect of	7.GM.4.1 Describe the properties of similarity, compare geometric figures for similarity, and determine scale factors resulting from dilations.
translations, reflections, rotations, and dilations on the attributes of two- dimensional figures on and off the coordinate plane.	7.GM.4.2 Apply proportions, ratios, and scale factors to solve problems involving scale drawings and to determine side lengths and areas of similar triangles and rectangles.
	7.GM.4.3 Graph and describe translations (with directional and algebraic instructions), reflections across the x- and y-axes, and rotations in 90° increments about the origin of figures on a coordinate plane, and determine the coordinates of the vertices of a figure after a transformation.



	Data & Probability (D)					
7.D.1 Interpret and analyze data, creating the most appropriate display, using a variety of tools.	7.D.1.1 Design simple experiments, collect data, and calculate measures of center (mean, median, and mode) and spread (range and interquartile range). Use these quantities to draw conclusions about the data collected and make predictions.					
	7.D.1.2 Use reasoning with proportions to display and interpret data in circle graphs (pie charts) and histograms.					
	7.D.1.3 Use technology to create and analyze box plots.					
7.D.2 Calculate and use proportional reasoning with probabilities to model and solve mathematical problems.	7.D.2.1 Determine the theoretical probability of an event using the ratio between the size of the event and the size of the sample space; represent probabilities as percents, fractions and decimals between 0 and 1.					
	7.D.2.2 Calculate probability as a fraction of sample space or as a fraction of area. Express probabilities as percents, decimals and fractions.					
	7.D.2.3 Use proportional reasoning to draw conclusions about and predict relative frequencies of outcomes based on theoretical probabilities.					



Develop a Deep and Flexible Conceptual Understanding	_		Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate		
	Numbers & Operations (N)								
PA.N.1 Read, write, comparant represent real numbers			evelop and apply the prope expressions.	erties of integer exponents, in	cluding $a^0 = 1$ (with $a \neq 0$), to	generate equivalent numerio	cal and algebraic		
them to solve problems in v contexts.	arious	PA.N.1.2 Ex	press and compare approxi	imations of very large and very	/ small numbers using scienti	fic notation.			
contexts.		PA.N.1.3 M	ultiply and divide numbers e	expressed in scientific notatior	n and express the answer in s	cientific notation.			
				bers; locate real numbers on a as an irrational number betwee			to 400 or, if it is not a		
			Algel	braic Reasoning & Algel	bra (A)				
PA.A.1 Explain the concept mathematical situations and	l distinguish	PA.A.1.1 Recognize that a function is a relationship between an independent variable and a dependent variable in which the value of the independent variable variable determines the value of the dependent variable.							
between the concepts of lin nonlinear functions.	ear and	PA.A.1.2 Use linear functions to represent and model mathematical situations.							
nommear functions.		PA.A.1.3 Identify a function as linear if it can be expressed in the form <i>y</i> = <i>mx</i> + <i>b</i> or if its graph is a non-vertical straight line.							
PA.A.2 Identify and justify li		PA.A.2.1 Represent linear functions with tables, verbal descriptions, symbols, and graphs; translate from one representation to another.							
functions using mathematic and situations; solve proble		PA.A.2.2 Identify, describe, and analyze linear relationships between two variables.							
involving linear functions an results in the original contex	d interpret	PA.A.2.3 Identify graphical properties of linear functions, including slope and intercepts. Know that the slope equals the rate of change, and that the y-intercept is zero when the function represents a proportional relationship.							
		PA.A.2.4 Predict the effect on the graph of a linear function when the slope or y-intercept changes. Use appropriate tools to examine these effects.							
		PA.A.2.5 So	olve problems involving linea	ar functions and interpret resu	lts in the original context.				
PA.A.3 Generate equivaler	nt numerical	PA.A.3.1 Use substitution to simplify and evaluate algebraic expressions.							
		PA.A.3.2 Justify steps in generating equivalent expressions by combining like terms and using order of operations (to include grouping symbols). Identify the properties used, including the properties of operations (associative, commutative, and distributive).							
PA.A.4 Represent and solve problems using mathematical models and		PA.A.4.1 Solve mathematical problems using linear equations with one variable where there could be one, infinitely many, or no solutions. Represent situations using linear equations and interpret solutions in the original context.							
situations with equations an inequalities involving linear	d	PA.A.4.2 Represent, write, solve, and graph problems leading to linear inequalities with one variable in the form $px + q > r$ and $px + q < r$, where p , q , and r are rational numbers.							
		PA.A.4.3 Re	epresent real-world situation	ns using equations and inequa	lities involving one variable.				



	Geometry & Measurement (GM)					
PA.GM.1 Apply the Pythagorean theorem to solve problems involving	PA.GM.1.1 Justify the Pythagorean theorem using measurements, diagrams, or dynamic software to solve problems in two dimensions involving right triangles.					
triangles.	PA.GM.1.2 Use the Pythagorean theorem to find the distance between any two points in a coordinate plane.					
PA.GM.2 Justify and use formulas to calculate surface area and volume of	PA.GM.2.1 Calculate the surface area of a rectangular prism using decomposition or nets. Use appropriate units (e.g., cm ²).					
three-dimensional figures.	PA.GM.2.2 Calculate the surface area of a cylinder, in terms of pi (Π) and using approximations for pi (Π), using decomposition or nets. Use appropriate units (e.g., cm ²).					
	PA.GM.2.3 Justify why base area (<i>B</i>) and height (<i>h</i>) in the formula <i>V=Bh</i> are multiplied to find the volume of a rectangular prism. Use appropriate units (e.g., cm ³).					
	PA.GM.2.4 Develop and use the formulas $V = (\pi r)^{s}h$ and $V = Bh$ to determine the volume of right cylinders, in terms of n and using approximations for pi (T). Justify why base area (B) and height (h) are multiplied to find the volume of a right cylinder. Use appropriate units (e.g., cm ³).					
	Data & Probability (D)					
PA.D.1 Display and interpret data in a variety of ways, including using scatter plots and approximate lines of best fit. Use	PA.D.1.1 Describe the impact that inserting or deleting a data point has on the mean and the median of a data set. Create data displays using technology to examine this impact.					
the line of best fit and average rate of change to make predictions and draw	PA.D.1.2 Explain how outliers affect measures of center and spread.					
conclusions about data.	PA.D.1.3 Collect, display, and interpret data using scatter plots. Use the shape of the scatter plot to find the informal line of best fit, make statements about the average rate of change, and make predictions about values not in the original data set. Use appropriate titles, labels, and units.					
PA.D.2 Calculate experimental probabilities and reason about probabilities to model and solve problems.	PA.D.2.1 Calculate experimental probabilities and represent them as percents, fractions, and decimals between 0 and 1. Use experimental probabilities to predict relative frequencies when actual probabilities are unknown.					
	PA.D.2.2 Determine how samples are chosen (randomness) to draw and support conclusions about generalizing a sample to a population, including identifying limitations and biases.					
	PA.D.2.3 Define, compare, and contrast the probabilities of dependent and independent events.					



Develop a Deep and Flexible Conceptual Understanding	Develop Accurate and Appropriate Procedural Fluency		Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate		
	Numbers & Operations (N)								
A1.N.1 Extend the underst		A1.N.1.1 W	rite square roots and cube r	oots of constants and monor	nial algebraic expressions in s	implest radical form.			
exponents to include squar and cube roots.	re roots	A1.N.1.2 A	dd, subtract, multiply, divide	e, and simplify square roots of	constants, rationalizing the d	enominator when necessary.			
			Algel	braic Reasoning & Alge	bra (A)				
A1.A.1 Represent and solv mathematical and real-worl	ld problems				represent, use and apply ma ce, statistics) and interpret the				
using linear equations, abso equations, and systems of e		A1.A.1.2 Sc	olve absolute value equation	s and interpret the solutions	in the original context.				
interpret solutions in the ori		A1.A.1.3 Analyze, use and apply mathematical models to solve problems involving systems of linear equations with a maximum of two variables by graphing, substitution, and elimination. Graphing calculators or other appropriate technology may be utilized. Interpret the solutions in the original context.							
A1.A.2 Represent and solv and mathematical problem		A1.A.2.1 Represent relationships using mathematical models with linear inequalities; solve the resulting inequalities, graph on a coordinate plane, and interpret the solutions.							
inequalities and compound interpret solutions in the or context.	inequalities;	A1.A.2.2 Represent relationships using mathematical models with compound and absolute value inequalities and solve the resulting inequalities by graphing and interpreting the solutions on a number line.							
A1.A.3 Create and evaluate	•	A1.A.3.1 Solve equations involving several variables for one variable in terms of the others.							
algebraic expressions and e using algebraic properties.	•	A1.A.3.2 Simplify polynomial expressions by adding, subtracting, or multiplying.							
		A1.A.3.3 Factor common monomial factors from polynomial expressions and factor quadratic expressions with a leading coefficient of 1.							
		A1.A.3.4 Evaluate linear, absolute value, rational, and radical expressions. Include applying a nonstandard operation such as x 🔿 y=2x+y							
-	A1.A.4 Analyze real-world and mathematical problems involving linear		A1.A.4.1 Analyze, use and apply mathematical models and other data sets (e.g., graphs, equations, two points, a set of data points) to calculate and interpret slope and the x- and y-intercepts of a line.						
equations.	5	A1.A.4.2 Analyze and interpret mathematical models involving lines that are parallel, perpendicular, horizontal, and vertical.							
			A1.A.4.3 Write the equation of the line given its slope and y-intercept, slope and one point, two points, x- and y-intercepts, or a set of data points.						
			A1.A.4.4 Express linear equations in slope-intercept, point-slope, and standard forms. Convert between these forms.						
		A1.A.4.5 Analyze and interpret associations between graphical representations and written scenarios.							



	Functions (F)				
A1.F.1 Understand functions as	A1.F.1.1 Distinguish between relations and functions.				
descriptions of covariation (how related quantities vary together) in real-world and mathematical problems.	A1.F.1.2 Identify the dependent variable, independent variable, domain and range given a function, equation, or graph. Identify restrictions on the domain and range in mathematical models.				
	A1.F.1.3 Write linear functions, using function notation, to represent mathematical models.				
	A1.F.1.4 Read and interpret the linear piecewise function, given a graph modeling a situation.				
	A1.F.1.5 Interpret graphs as being discrete or continuous.				
A1.F.2 Recognize and understand that families of functions are defined by their	A1.F.2.1 Distinguish between linear and nonlinear (including exponential) functions. Understand that linear functions grow by equal intervals (arithmetic) and that exponential functions grow by equal factors over equal intervals (geometric).				
characteristics.	A1.F.2.2 Recognize the parent functions $f(x) = x$ and $f(x) = x $. Predict the effects of vertical and horizontal transformations $f(x + c)$ and $f(x) + c$, algebraically and graphically.				
A1.F.3 Represent functions in multiple	A1.F.3.1 Identify and generate equivalent representations of linear functions, graphs, tables, and real-world situations.				
ways and use the representation to interpret real-world and mathematical problems.	A1.F.3.2 Use function notation; evaluate a function, including nonlinear, at a given point in its domain algebraically and graphically. Interpret the results in terms of the original context.				
	A1.F.3.3 Add, subtract, and multiply functions using function notation.				
	Data & Probability (D)				
A1.D.1 Display, describe, and compare data. For linear relationships, make	A1.D.1.1 Display, describe, and compare data sets using summary statistics (central tendency and spread (range)). Utilize technology (e.g., spreadsheets, calculators) to display data and calculate summary statistics.				
predictions, and assess the reliability of those predictions.	A1.D.1.2 Collect data and analyze scatter plots for patterns, linearity, and outliers.				
	A1.D.1.3 Make predictions based upon the linear regression, and use the correlation coefficient to assess the reliability of those predictions using graphing technology.				
A1.D.2 Calculate probabilities, and apply probability concepts.	A1.D.2.1 Apply simple counting procedures (factorials, permutations, combinations, and tree diagrams) to determine sample size, sample space, and calculate probabilities.				
	A1.D.2.2 Given a Venn diagram, determine the probability of the union of events, the intersection of events, and the complement of an event. Understand the relationships between these concepts and the words "AND," "OR," and "NOT."				
	A1.D.2.3 Use simulations and experiments to calculate experimental probabilities.				
	A1.D.2.4 Apply probability concepts to real-world situations to make informed decisions.				



Develop a Deep and Flexible Conceptual Understanding	Develop Accurate and Appropriate Procedural Fluency		Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate		
	Geometry: Reasoning & Logic (G.RL)								
G.RL.1 Use appropriate to		G.RL.1.1 Us	e undefined terms, definitio	ns, postulates, and theorems	in logical arguments/proofs.				
logic, including algebraic r evaluate mathematical arg				based on a set of conditions nt and its inverse, converse,	using inductive and deductive and contrapositive.	e reasoning. Recognize the lo	gical relationships		
		G.RL.1.3 As	sess the validity of a logical a	argument and give countere	xamples to disprove a stateme	ent.			
			Geometry	v: Two-Dimensional Sh	apes (G.2D)				
G.2D.1 Discover, evaluate		G.2D.1.1 Us	e properties of parallel lines	s cut by a transversal to deter	mine angle relationships and	solve problems.			
the relationships between and polygons to solve real mathematical problems; exp	-world and press proofs	G.2D.1.2 Use the angle relationships formed by lines cut by a transversal to determine if the lines are parallel and verify, using algebraic and deductive proofs.							
in a form that clearly justific reasoning (e.g., two-colum paragraph proofs, flowcha	nn proofs,	G.2D.1.3 Apply the properties of angles (corresponding, exterior, interior, vertical, complementary, supplementary) to solve problems using mathematical models, algebraic reasoning, and proofs.							
paragraph proois, nowena		G.2D.1.4 Apply theorems involving the interior and exterior angle sums of polygons to solve problems using mathematical models, algebraic reasoning, and proofs.							
		G.2D.1.5 Apply the properties of special quadrilaterals (square, rectangle, trapezoid, isosceles trapezoid, rhombus, kite, parallelogram) to solve problems involving angle measures and segment lengths using mathematical models, algebraic reasoning, and proofs.							
		G.2D.1.6 Use coordinate geometry and algebraic reasoning to represent and analyze line segments and polygons, including determining lengths, midpoints, and slopes of line segments.							
		G.2D.1.7 Apply the properties of polygons, and use them to represent and apply mathematical models involving perimeter and area (e.g., triangles, special quadrilaterals, regular polygons up to 12 sides, composite figures).							
		G.2D.1.8 Apply the properties of congruent or similar polygons to solve problems using mathematical models and algebraic and logical reasoning.							
		G.2D.1.9 Construct logical arguments to prove triangle congruence (SSS, SAS, ASA, AAS and HL).							
		G.2D.1.10 Construct logical arguments to prove triangle similarity (AA, SSS, SAS).							
					ansformations in two dimensi lving figures on a coordinate				



	Geometry: Three-Dimensional Shapes (G.3D)				
G.3D.1 Solve real-world and mathematical problems involving three-	G.3D.1.1 Represent, use, and apply mathematical models and other tools (e.g., nets, measuring devices, formulas) to solve problems involving surface area and volume of three-dimensional figures (prisms, cylinders, pyramids, cones, spheres, composites of these figures).				
dimensional figures.	G.3D.1.2 Use ratios derived from similar three-dimensional figures to make conjectures, generalize, and to solve for unknown values such as angles, side lengths, perimeter, and circumference of a face, area of a face, and volume.				
	Geometry: Circles (G.C)				
G.C.1 Solve real-world and mathematical problems using the properties of circles.	G.C.1.1 Apply the properties of circles to solve problems involving circumference and area, using approximate values and in terms of pi, using algebraic and logical reasoning.				
	G.C.1.2 Use the distance and midpoint formula, where appropriate, to recognize and write the radius <i>r</i> , center (<i>h</i> , <i>k</i>), and standard form of the equation of a circle $(x - h)^2 + (y - k)^2 = r^2$ with and without graphs.				
	G.C.1.3 Apply the properties of circles and relationships among angles; arcs; and distances in a circle among radii, chords, secants, and tangents to solve problems using algebraic and logical reasoning.				
	Geometry: Right Triangle Trigonometry (G.RT)				
G.RT.1 Apply mathematical relationships of right triangles and	G.RT.1.1 Apply the distance formula, the Pythagorean theorem, and the Pythagorean theorem converse (approximate and exact values, including Pythagorean triples) to solve problems, using algebraic and logical reasoning and mathematical models.				
trigonometric ratios to solve real-world and mathematical problems.	G.RT.1.2 Verify and apply properties of right triangles, including properties of 45-45-90 and 30-60-90 triangles, to solve problems using algebraic and logical reasoning.				
	G.RT.1.3 Use the definition of the trigonometric functions to determine the sine, cosine, and tangent ratio of an acute angle in a right triangle. Apply the inverse trigonometric functions to find the measure of an acute angle in right triangles.				
	G.RT.1.4 Apply the trigonometric functions as ratios (sine, cosine, tangent) to find side lengths in right triangles in mathematical models, including the coordinate plane.				



Develop a Deep and Flexible Conceptual Understanding			Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate	
	Numbers & Operations (N)							
A2.N.1 Extend the unders	•	A2.N.1.1 F	Find the value of <i>i</i> ⁿ for any wh	ole number <i>n</i> .				
numbers and operations to complex numbers, radical	expressions,	A2.N.1.2 S	implify, add, subtract, multip	ly, and divide complex numb	ers.			
and expressions written wi exponents.	ith rational	A2.N.1.3	Inderstand and apply the rela	ationship between rational e>	ponents to integer exponent	s and radicals to solve proble	ms.	
A2.N.2 Extend the unders		A2.N.2.1	Jse matrices to organize and i	represent data. Identify the o	rder (dimension) of a matrix.			
numbers and operations to	o matrices.	A2.N.2.2	Jse addition, subtraction, and	l scalar multiplication of matr	ces to solve problems.			
			Algel	braic Reasoning & Alge	bra (A)			
A2.A.1 Represent and solv mathematical and real-wor	rld problems	A2.A.1.1 Use mathematical models to represent quadratic relationships and solve using factoring, completing the square, the quadratic formula, and various methods (including graphing calculator or other appropriate technology). Find non-real roots when they exist.						
using nonlinear equations, linear equations, and syste inequalities; interpret the s	ems of linear	A2.A.1.2 Use mathematical models to represent exponential relationships, such as compound interest, depreciation, and population growth. Solve these equations algebraically or graphically (including graphing calculator or other appropriate technology).						
original context.		A2.A.1.3 Solve one-variable rational equations and check for extraneous solutions.						
		A2.A.1.4 Solve polynomial equations with real roots using various methods (e.g., polynomial division, synthetic division, using graphing calculators or other appropriate technology).						
		A2.A.1.5 Solve square and cube root equations with one variable, and check for extraneous solutions.						
		A2.A.1.6 Solve common and natural logarithmic equations using the properties of logarithms.						
		A2.A.1.7 Represent and evaluate mathematical models using systems of linear equations with a maximum of three variables. Graphing calculators or other appropriate technology may be used.						
		A2.A.1.8 Use tools to solve systems of equations containing one linear equation and one quadratic equation. Graphing calculators or other appropriate technology may be used.					ators or other appropriate	
A2.A.1.9 Solve systems of linear inequalities in two variables, with a maximum of three inequalities; graph and interpret the solution plane. Graphing calculators or other appropriate technology may be used.						utions on a coordinate		



A2.A.2 Generate and evaluate equivalent algebraic expressions and	A2.A.2.1 Factor polynomial expressions including, but not limited to, trinomials, differences of squares, sum and difference of cubes, and factoring by grouping, using a variety of tools and strategies.						
equations using various strategies.	A2.A.2.2 Add, subtract, multiply, divide, and simplify polynomial expressions.						
	A2.A.2.3 Add, subtract, multiply, divide, and simplify rational expressions.						
	A2.A.2.4 Recognize that a quadratic function has different equivalent representations $[f(x) = ax^2 + bx + c, f(x) = a(x - h)^2 + k,$ and $f(x) = a(x - p)(x - q)]$. Identify and use the mathematical model that is most appropriate to solve problems.						
	A2.A.2.5 Rewrite algebraic expressions involving radicals and rational exponents using the properties of exponents.						
A2.A.3 Represent and solve	A2.A.3.1 Recognize that arithmetic sequences are linear using equations, tables, graphs, and verbal descriptions. Using the pattern, find the next term.						
mathematical and real-world problems involving arithmetic and	A2.A.3.2 Recognize that geometric sequences are exponential using equations, tables, graphs, and verbal descriptions. Given the formula $f(x) = a(r)^x$, find the next term and define the meaning of a and r within the context of the problem.						
geometric sequences and series.	A2.A.3.3 Solve problems that can be modeled using arithmetic sequences or series given the <i>n</i> th terms and sum formulas. Graphing calculators or other appropriate technology may be used.						
	A2.A.3.4 Solve problems that can be modeled using finite geometric sequences and series given the <i>n</i> th terms and sum formulas. Graphing calculators or other appropriate technology may be used.						
	Functions (F)						
A2.F.1 Understand functions as descriptions of covariation (how related	A2.F.1.1 Use algebraic, interval, and set notations to specify the domain and range of various types of functions, and evaluate a function at a given point in its domain.						
quantities vary together).	A2.F.1.2 Identify the parent forms of exponential, radical (square root and cube root only), quadratic, and logarithmic functions. Predict the effects of transformations [$f(x + c)$, $f(x) + c$, $f(cx)$, and $cf(x)$] algebraically and graphically.						
	A2.F.1.3 Graph a quadratic function. Identify the domain, range, x- and y-intercepts, maximum or minimum value, axis of symmetry, and vertex using various methods and tools that may include a graphing calculator or appropriate technology.						
	A2.F.1.4 Graph exponential and logarithmic functions. Identify the domain, range, asymptotes, and x- and y-intercepts using various methods and tools that may include calculators or other appropriate technology. Recognize exponential decay and growth graphically and algebraically.						
	A2.F.1.5 Analyze the graph of a polynomial function by identifying the domain, range, intercepts, zeros, relative maxima, relative minima, and intervals of increase and decrease.						
	A2.F.1.6 Graph a rational function and identify the domain (including holes), range, x- and y-intercepts, vertical and horizontal asymptotes, using various methods and tools that may include a graphing calculator or other appropriate technology (excluding slant or oblique asymptotes).						
	A2.F.1.7 Graph a radical function (square root and cube root only). Identify the domain, range, and x- and y-intercepts using various methods and tools that may include a graphing calculator or other appropriate technology.						



A2.F.1 <i>continued</i> Understand functions as descriptions of covariation (how related quantities vary together).	A2.F.1.8 Graph piecewise functions with no more than three branches (linear, quadratic, or exponential). Analyze the function by identifying the domain, range, intercepts, and intervals for which it is increasing, decreasing, and constant using various methods and tools (e.g., graphing calculator, other appropriate technology).					
	A2.F.1.9 Recognize whether a discrete or continuous graphical representation is appropriate to create a graph based upon a mathematical model.					
A2.F.2 Analyze functions through	A2.F.2.1 Add, subtract, multiply, and divide functions using function notation and recognize domain restrictions.					
algebraic combinations, compositions, and inverses if they exist.	A2.F.2.2 Combine functions by composition and recognize that $g(x) = f^{-1}(x)$, the inverse function of $f(x)$, if and only if $f(g(x)) = g(f(x)) = x$.					
	A2.F.2.3 Find and graph the inverse of a function, if it exists, in mathematical models. Know that the domain of a function f is the range of the inverse function f^{-1} and the range of the function f is the domain of the inverse function f^{-1}					
	A2.F.2.4 Apply the inverse relationship between exponential and logarithmic functions to convert from one form to another.					
	Data & Probability (D)					
A2.D.1 Display, describe, and compare	A2.D.1.1 Use the mean and standard deviation of a data set to create a normal distribution (bell-shaped curve).					
data. For linear and nonlinear relationships, make predictions and	A2.D.1.2 Collect data and use scatter plots to analyze patterns and describe linear, exponential, or quadratic relationships between two variables.					
assess the reliability of those predictions.	A2.D.1.3 Make predictions based upon the regression equation (linear, exponential, or quadratic), and use the correlation coefficient to assess the reliability of those predictions using graphing technology.					
A2.D.2 Analyze statistical thinking to draw inferences, make predictions, and justify conclusions.	A2.D.2.1 Evaluate reports by making inferences, justifying conclusions, and determining appropriateness of data collection methods. Show how graphs and data can be distorted to support different points of view.					
	A2.D.2.2 Identify and explain misleading conclusions and graphical representations of data sets.					
	A2.D.2.3 Differentiate between correlation and causation when describing the relationship between two variables.					



Develop a Deep and Flexible Conceptual Understanding	Conceptual and Appropriate		Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate		
	Functions (F)								
PC.F.1 Analyze functions ar	nd relations.	-		nction defined by an expressi that models a relationship be					
		PC.F.1.3 In	terpret characteristics of grap	phs and tables for a function t	hat models a relationship be	tween two quantities in terms	of the quantities.		
		PC.F.1.4 D	escribe end behavior, asymp	ototic behavior, and points of	discontinuity.				
				inverse. Algebraically and gr d find the inverse on the rest		define any restrictions on the	domain that meet the		
PC.F.2 Build functions to m validate relationships among		PC.F.2.1 Model relationships through composition, and attend to the restrictions of the domain.							
	g functions.	PC.F.2.2 Rewrite a function as a composition of functions.							
		PC.F.2.3 Interpret the meanings of quantities involving functions and their inverses.							
		PC.F.2.4 V	erify by analytical methods th	nat one function is the inverse	of another.				
PC.F.3 Predict and verify so involving functions.	olutions	PC.F.3.1 Predict solutions involving functions that are quadratic, polynomial of higher order, rational, exponential, and logarithmic.							
involving functions.		PC.F.3.2 Graphically verify solutions involving functions that are quadratic, polynomial of higher order, rational, exponential, and logarithmic.							
		PC.F.3.3 Algebraically verify solutions involving functions that are quadratic, polynomial of higher order, rational, exponential, and logarithmic.							
	Conic Sections (CS)								
PC.CS.1 Investigate conic se	ections.	PC.CS.1.1 Model real-world situations which involve conic sections.							
		PC.CS.1.2 Identify key features of conic sections (foci, directrix, radii, axes, asymptotes, center) graphically and algebraically.							
		PC.CS.1.3 Sketch a graph of a conic section using its key features.							
		PC.CS.1.4 Write the equation of a conic section given its key features.							
		PC.CS.1.5	Given the equation $ax^2 + by^2$	+ cx + dy + e = 0, determine	if the equation represents a o	circle, ellipse, parabola, or hy	perbola.		



	Trigonometry (T)					
PC.T.1 Make sense of the unit circle and	PC.T.1.1 Draw and recognize angles in standard position using radian measure, and determine the quadrant of the terminal side.					
its relationship to the graphs of trigonometric functions.	PC.T.1.2 Convert radian measure to degree measure and vice-versa.					
	PC.T.1.3 Find the length of an arc and the area of a sector on a circle.					
	PC.T.1.4 Use special triangles to determine geometrically the values of sine, cosine, tangent for $\frac{\pi}{3}$, $\frac{\pi}{4}$, and $\frac{\pi}{6}$, and use the unit circle to express the values of sine, cosine, and tangent for $\pi - x$, $\pi + x$, and $2\pi - x$ in terms of their values for x, where x is any real number.					
	PC.T.1.5 Use reference angles to determine the terminal point $P(x, y)$ on the unit circle for a given angle.					
	PC.T.1.6 Estimate trigonometric values of any angle.					
	PC.T.1.7 Apply the properties of a unit circle to explain symmetry (odd and even) and periodicity of trigonometric functions.					
	PC.T.1.8 Graph of all six trigonometric functions, identifying key features.					
	PC.T.1.9 Describe and analyze the relationships of the properties of a unit circle.					
PC.T.2 Apply trigonometric concepts	PC.T.2.1 Create models for situations involving trigonometry.					
beyond the right triangle.	PC.T.2.2 Apply the Law of Sines and Law of Cosines to solve problems.					
	PC.T.2.3 Use trigonometry to find the area of triangles.					
	PC.T.2.4 Use inverse functions to solve trigonometric equations; evaluate the solution and interpret them in terms of context.					
PC.T.3 Verify trigonometric identities and	PC.T.3.1 Algebraically manipulate the structure of a trigonometric expression to identify ways to rewrite it.					
solve equations.	PC.T.3.2 Choose and produce an equivalent form of an expression to explain the properties of the quantity represented by the expression.					
	PC.T.3.3 Graphically and algebraically verify solutions to trigonometric equations.					
PC.T.4 Explore complex numbers.	PC.T.4.1 Use the relation $i^2 = -1$ and the mathematical properties to add, subtract, and multiply complex numbers.					
	PC.T.4.2 Find the conjugate of a complex number in rectangular forms and quotients of complex numbers.					
	PC.T.4.3 Solve quadratic equations in one variable that have complex solutions.					



Develop a Deep and Flexible Conceptual Understanding	Develop Acc Appropriate Fluer	Procedural	Develop Strategies for Problem Solving	Develop Mathematical Reasoning	Develop a Productive Mathematical Disposition	Develop the Ability to Make Conjectures, Model, and Generalize	Develop the Ability to Communicate	
Statistical Questions (Q)								
S.Q.1 Understand the distinction between mathematical models and statistical models.		 S.Q.1.1 Distinguish among different sources of variability, including measurement, natural, induced, and sampling variability. S.Q.1.2 Formulate meaningful statistical questions to clarify the problem at hand. 						
S.Q.2 Distinguish between the distribution of a population, a distribution of sample data, and a sampling distribution.		 S.Q.2.1 Distinguish between sample statistics and population parameters. S.Q.2.2 Recognize a population distribution has fixed values of its parameters and that these parameter values are typically unknown. S.Q.2.3 Recognize that a sample data distribution is taken from a population distribution, and the data distribution is what is seen in practice. S.Q.2.4 Recognize a sampling distribution is the distribution of a sample statistic (e.g., sample mean, sample proportion) obtained from repeated 						
S.Q.3 Identify differences between categorical and quantitative data.		samples. S.Q.3.1 Determine whether categorical or quantitative data is appropriate to answer a statistical question. S.Q.3.2 Compare and contrast different potential graphical or visual representations given the same data set.						
S.DC.1 Distinguish among different types of study designs for collecting data, and know the scope of inference for each design type.		Data Collection (DC) S.DC.1.1 Distinguish among sample surveys, experiments, and observational studies. S.DC.1.2 Compare and contrast the benefits of different sampling techniques. S.DC.1.3 Determine the appropriate scope of inference for generalizing results.						
		S.DC.1.4 Explain how sample size impacts the precision with which generalizations can be made. S.DC.1.5 Determine when a cause-and-effect inference can be drawn from an association, based on how the data were collected.						
S.DC.2 Identify common sources of bias and the role of randomization in study design.		 S.DC.2.1 Explain how randomization and sources of bias impact the results of a study. S.DC.2.2 Understand the different roles of random selection and random assignment in study design. 						



	Data Analysis (DA)				
S.DA.1 Use distributions of quantitative and categorical data to identify the key features of the data collected in context.	S.DA.1.1 Summarize and represent the distribution for univariate quantitative data by describing and analyzing the shape of the distribution, the measures of center for the distribution, the patterns in variability for the distribution, and any outliers, gaps, or other unusual features in the distribution.				
	S.DA.1.2 Select and create an appropriate display (e.g., dot plots, histograms, box plots) for univariate data.				
	S.DA.1.3 Use statistics appropriate to the shape of the data distribution to compare center and variability of two or more different data sets.				
	S.DA.1.4 Describe and analyze the distribution of univariate categorical data.				
S.DA.2 Use the mean and standard deviation of a data set to fit it to a normal distribution and to estimate population percentages.	S.DA.2.1 Use calculators, computers, or tables to estimate areas under the normal curve. Recognize that there are data sets for which such a procedure is not appropriate.				
S.DA.3 Compare two or more groups by analyzing distributions.	S.DA.3.1 Construct appropriate parallel graphical displays of distributions.				
	S.DA.3.2 Use numerical attributes of distributions to make comparisons between distributions.				
S.DA.4 Analyze associations between two variables.	S.DA.4.1 Create two-way tables for bivariate categorical data and analyze for possible associations between the two categories using marginal, joint, and conditional frequencies.				
	S.DA.4.2 Make predictions and draw conclusions from regression models (linear, exponential, quadratic) from two-variable quantitative data.				
	S.DA.4.3 Analyze scatter plots for patterns, linearity, outliers, and influential points.				
	S.DA.4.4 Using technology, compute and interpret the correlation coefficient.				
	S.DA.4.5 Understand the implications of extrapolating data to make predictions.				
S.DA.5 Make statistical inferences and	S.DA.5.1 Construct and interpret confidence intervals for the mean of a normally distributed population and for a population proportion.				
evaluate claims from studies.	S.DA.5.2 Explain how a sample statistic and a confidence level are used in the construction of a confidence interval.				
	S.DA.5.3 Explain how changes in the sample size, confidence level, and standard error affect the margin of error of a confidence interval.				
	S.DA.5.4 Construct a confidence interval for the mean of a normally distributed population (with a known standard deviation) and for a population proportion. Use confidence intervals to evaluate claims.				
	S.DA.5.5 Use confidence intervals to evaluate claims for a single population parameter.				



Interpretation of Results (IR)					
S.IR.1 Interpret and communicate the results of a statistical analysis in context.	S.IR.1.1 Recognize when the difference between two sample proportions or two sample means is due to random variation or if the difference is statistically significant.				
	S.IR.1.2 Understand the concept of a confidence interval, including the interpretation of confidence level, margin of error, and statistical significance.				
	S.IR.1.3 Develop inferences or predictions to construct resulting decisions or recommendations.				
	S.IR.1.4 Create and evaluate recommendations for areas of future research.				
S.IR.2 Evaluate practical implications of statistical significance or lack thereof.	S.IR.2.1 Develop and critique arguments for practical implications based on statistical significance.				
	S.IR.2.2 Identify potential lurking variables which may explain an association between two variables.				
S.IR.3 Evaluate real-world claims and	S.IR.3.1 Evaluate strengths and weaknesses in the studies or methods used to generate data.				
conclusions.	S.IR.3.2 Evaluate the statistical validity of claims made.				
	Probability (P)				
S.P.1 Connect basic probability concepts to statistical analysis.	S.P.1.1 Describe events as subsets of a sample space.				
	S.P.1.2 Describe the relationship between theoretical and empirical probabilities using the Law of Large Numbers.				
	S.P.1.3 Use counting techniques (e.g., permutations and combinations) to solve mathematical and real-world problems, including determining probabilities of compound events.				
S.P.2 Determine probabilities, including joint probabilities, conditional probabilities, probabilities of independent events, and probabilities of dependent events. Interpret the results.	S.P.2.1 Understand that two events, A and B, are independent if the probability of A and B occurring together is the product of their probabilities, and this characterization to determine if two events are independent.				
	S.P.2.2 Understand and calculate the conditional probability of A given B as P(A and B)/P(B).				
	S.P.2.3 Interpret independence of A and B as saying that the conditional probability of A, given B, is the same as the probability of A.				
S.P.3 Use probability to make decisions.	S.P.3.1 Analyze decisions and strategies using probability concepts and expected values.				
	S.P.3.2 Analyze decisions about statistical significance based on reported p-values.				